

Parsing

Left-Corner Parsing

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Table of contents

- 1 Motivation
- 2 Algorithm
- 3 Look-ahead
- 4 Chart Parsing

Motivation

Problems with pure TD/BU approaches:

- Top-Down does not check whether the actual input corresponds to the predictions made.
- Bottom-Up does not check whether the recognized constituents correspond to anything one might predict starting from S.

Mixed approaches help to overcome these problems:

- Left-Corner Parsing parses parts of the tree top down, parts bottom-up.
- Earley-Parsing is a chart-based combination of top-down predictions and bottom-up completions.

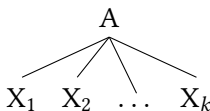
Idea

In a production $A \rightarrow X_1 \dots X_k$, the first righthand side element X_1 is called the **left corner** of this production.

Notation: $\langle A, X_1 \rangle \in LC$.

Idea:

- Parse the left corner bottom-up while parsing X_2, \dots, X_k top-down.
- In other words, in order to predict the subtree



a parse tree for X_1 must already be there.

Algorithm (1)

We assume a CFG without ε -productions and without loops.

We need the following three stacks:

- a stack Γ_{compl} containing completed elements that can be used as potential left corners for applying new productions.
Initial value: w
- a stack Γ_{td} containing the top-down predicted elements of a rhs (i.e., the rhs without the left corner)
Initial value: S
- a stack Γ_{lhs} containing the lhs categories that are waiting to be completed. Once all the top-down predicted rhs symbols are completed, the category is moved to Γ_{compl} .
Initial value: ε

Algorithm (2)

Item form $[\Gamma_{compl}, \Gamma_{td}, \Gamma_{lhs}]$ with

- $\Gamma_{compl} \in (N \cup T)^*$,
- $\Gamma_{td} \in (N \cup T \cup \{\$\})^*$ where $\$$ is a new symbol marking the end of a rhs,
- $\Gamma_{lhs} \in N^*$.

Whenever the symbols X_2, \dots, X_k from a rhs are pushed onto Γ_{td} , they are preceded by $\$$ to mark the end of a rhs (i.e., the point where a category can be completed).

Axiom: $\frac{}{[w, S, \varepsilon]}$

Algorithm (3)

Reduce can be applied if the top of Γ_{compl} is the left corner X_1 of some rule $A \rightarrow X_1 X_2 \dots X_k$. Then X_1 is popped, $X_2 \dots X_k \$$ is pushed onto Γ_{td} and A is pushed onto Γ_{lhs} :

$$\text{Reduce: } \frac{[X_1 \alpha, B \beta, \gamma]}{[\alpha, X_2 \dots X_k \$ B \beta, A \gamma]} \quad A \rightarrow X_1 X_2 \dots X_k \in P, B \neq \$$$

Once the entire righthand side has been completed (top of Γ_{td} is $\$$), the completed category is moved from Γ_{lhs} to Γ_{compl} :

$$\text{Move: } \frac{[\alpha, \$ \beta, A \gamma]}{[A \alpha, \beta, \gamma]} \quad A \in N$$

Algorithm (4)

A completed category can be a left corner (then reduce is applied) or it can be the next symbol on the Γ_{td} stack, then both can be popped:

Remove: $\frac{[X\alpha, X\beta, \gamma]}{[\alpha, \beta, \gamma]}$

The recognizer is successful if $\Gamma_{compl} = \Gamma_{td} = \Gamma_{lhs} = \varepsilon$:

Goal item: $[\varepsilon, \varepsilon, \varepsilon]$

Algorithm (5)

Example: Left Corner Parsing

Productions:

$S \rightarrow aSa \mid bSb \mid c$

input $w = abcba$.

Γ_{compl}	Γ_{td}	Γ_{lhs}	operation
$abcba$	S	ϵ	
$bcba$	$SaSS$	S	reduce
cba	$SbSSaSS$	SS	reduce
ba	$SSbSSaSS$	SSS	reduce
Sba	$SbSSaSS$	SS	move
ba	$bSSaSS$	SS	remove
a	$SSaSS$	SS	remove
Sa	$SaSS$	S	move
a	aSS	S	remove
ϵ	SS	S	remove
S	S	ϵ	move
ϵ	ϵ	ϵ	remove

Algorithm (6)

Problematic for left-corner parsing:

- ε -productions: there is no left corner that can trigger a reduce step with an ε -production. If we allow ε -productions to be predicted in reduce steps without a left corner, we would add them an infinite number of times.
- loops: as in the LL-parsing case, loops can cause an infinite sequence of reduce and move steps. This problem is already avoided with the item-based formulation since we would only try to create the same items again.

Both problems can be overcome using the chart-based version with dotted productions described later.

Look-ahead (1)

Idea:

- build the reflexive transitive closure LC^* of the left corner relation LC ,
- before applying *reduce*, check whether the top of Γ_{td} stands in the relation LC^* to the lhs of the new production we predict:

Reduce:

$$\frac{[X_1\alpha, B\beta, \gamma]}{[\alpha, X_2 \dots X_k \beta, A\gamma]} \quad A \rightarrow X_1X_2 \dots X_k \in P, \langle B, A \rangle \in LC^*$$

Difference between LC^* and *First*: LC^* for a given non-terminal can be non-terminals and terminals, while the *First* sets contain only terminals.

$$LC^* = \{ \langle A, X \rangle \mid A \xRightarrow{*} X\alpha \}$$

Look-ahead (2)

Example:

VP \rightarrow V NP, VP \rightarrow VP PP, V \rightarrow sees,

NP \rightarrow Det N, Det \rightarrow the, N \rightarrow N PP, N \rightarrow girl, N \rightarrow telescope,

PP \rightarrow P NP, P \rightarrow with

LC:

\langle VP, V \rangle , \langle VP, VP \rangle , \langle V, sees \rangle \langle NP, Det \rangle , \langle Det, the \rangle ,
 \langle N, N \rangle , \langle N, girl \rangle , \langle N, telescope \rangle , \langle PP, P \rangle , \langle P, with \rangle

*LC** = *LC* \cup :

$\{ \langle$ VP, sees \rangle , \langle V, V \rangle , \langle NP, NP \rangle , \langle NP, the \rangle ,
 \langle PP, PP \rangle , \langle PP, with \rangle , \langle P, P \rangle $\}$

Chart Parsing (1)

Problem of left corner parsing: non-deterministic.

In order to avoid computing partial results several times, we can use tabulation, i.e., adopt chart parsing.

Items we need to tabulate:

- Completely recognized categories: passive items $[X, i, l]$
- Partially recognized productions: active items $[A \rightarrow \alpha \bullet \beta, i, l]$
with $\alpha \in (N \cup T)^+, \beta \in (N \cup T)^*$

(i index of first terminal in yield, l length of the yield)

Chart Parsing (2)

Let us again assume a CFG without ε -productions.

We start with the initial items $[w_i, i, 1]$.

The operations *reduce*, *remove* and *move* are then as follows:

- Reduce: If $[X_1, i, l]$ and $A \rightarrow X_1X_2 \dots X_k \in P$, then we add $[A \rightarrow X_1 \bullet X_2 \dots X_k, i, l]$.
- Move: If $[A \rightarrow X_1X_2 \dots X_k \bullet, i, l]$, then we add $[A, i, l]$
- Remove: If $[X, i, l]$ and $[A \rightarrow \alpha \bullet X\beta, j, i - j]$ then we add $[A \rightarrow \alpha X \bullet \beta, j, i - j + l]$.

Chart Parsing (3)

Parsing Schema:

$$\text{Scan: } \frac{}{[w_i, i, 1]} \quad 1 \leq i \leq n$$

$$\text{Reduce: } \frac{[X, i, l]}{[A \rightarrow X \bullet \alpha, i, l]} \quad A \rightarrow X\alpha \in P$$

$$\text{Remove: } \frac{[A \rightarrow \alpha \bullet X\beta, i, l_1], [X, j, l_2]}{[A \rightarrow \alpha X \bullet \beta, i, l_1 + l_2]} \quad j = i + l_1$$

$$\text{Move: } \frac{[A \rightarrow \alpha X \bullet, i, l]}{[A, i, l]}$$

Goal item: $[S, 1, n]$.

(This is actually the same algo as the CYK with dotted productions seen earlier in the course, except for different names of the rules and a different use of indices.)

Chart Parsing (4)

Example: Left Corner Chart Parsing

Productions: $S \rightarrow aSa \mid bSb \mid c$, input $w = abcba$.

item(s)	rule	antecedens items
$[a, 1, 1], [b, 2, 1], [c, 3, 1], [b, 4, 1], [a, 5, 1]$ (axioms)		
$[S \rightarrow a \bullet Sa, 1, 1]$	reduce	$[a, 1, 1]$
$[S \rightarrow b \bullet Sb, 2, 1]$	reduce	$[b, 2, 1]$
$[S \rightarrow c \bullet, 3, 1]$	reduce	$[c, 3, 1]$
$[S \rightarrow a \bullet Sb, 4, 1]$	reduce	$[b, 4, 1]$
$[S \rightarrow b \bullet Sa, 5, 1]$	reduce	$[a, 5, 1]$
$[S, 3, 1]$	move	$[S \rightarrow c \bullet, 3, 1]$
$[S \rightarrow bS \bullet b, 2, 2]$	remove	$[S \rightarrow b \bullet Sb, 2, 1], [S, 3, 1]$
$[S \rightarrow bSb \bullet, 2, 3]$	remove	$[S \rightarrow bS \bullet b, 2, 2], [b, 4, 1]$
$[S, 2, 3]$	move	$[S \rightarrow bSb \bullet, 2, 3]$
$[S \rightarrow aS \bullet a, 1, 4]$	remove	$[S \rightarrow a \bullet Sa, 1, 1], [S, 2, 3]$
$[S \rightarrow aSa \bullet, 1, 5]$	remove	$[S \rightarrow aS \bullet a, 1, 4], [a, 5, 1]$
$[S, 1, 5]$	move	$[S \rightarrow aSa \bullet, 1, 5]$

Conclusion

- The left corner of a production is the first element of its rhs.
- Predict a production only if its left corner has already been found.
- In general non-deterministic.
- Problematic for ε -productions and loops.
- Can be implemented as a chart parser with passive and active items.
- In the chart parser, ε -productions can be dealt with (they require an additional Scan- ε rule) and loops are no longer a problem.