
Mildly Context-Sensitive Grammar

Formalisms:

Tree Substitution Grammars

Laura Kallmeyer
Heinrich-Heine-Universität Düsseldorf
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Grammar Formalisms 1 Tree Substitution Grammars

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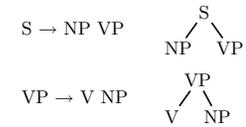
Overview

1. Motivation
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3. Equivalence of CFG and TSG
4. Applications

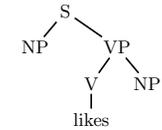
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Motivation

- In a CFG, the elements in the grammars represent very small syntactic trees.



- From a linguistic point of view, in particular in a lexicalized grammar, we would like entire constructions to be our elementary building blocks.



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Tree Substitution Grammars (1)

This leads to the definition of [Tree Substitution Grammars \(TSG\)](#).

- A TSG consists of a set of syntactic trees.
- From these trees, larger trees can be built by replacing a non-terminal leaf with a new tree whose root node is labeled with the same non-terminal.
- This operation is called [substitution](#).

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Tree Substitution Grammars (2)

Definition 1 (Substitution)

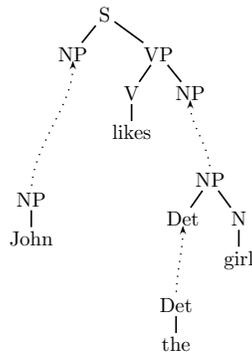
Let $\gamma = \langle V, E, r \rangle$ and $\gamma' = \langle V', E', r' \rangle$ be syntactic trees with $V \cap V' = \emptyset$ and $v \in V$. $\gamma[v, \gamma']$, the result of *substituting* γ' into γ at node v is defined as follows:

- if v is not a leaf or $l(v) \neq l(r')$, then $\gamma[v, \gamma']$ is undefined;
- otherwise, $\gamma[v, \gamma'] = \langle V'', E'', r'' \rangle$ with $V'' = V \cup V' \setminus \{v\}$ and $E'' = (E \setminus \{\langle v_1, v_2 \rangle \mid v_2 = v\}) \cup E' \cup \{\langle v_1, r' \rangle \mid \langle v_1, v \rangle \in E\}$.

Furthermore, $v_1 \prec v_2$ in $\gamma[v, \gamma']$ iff either $v_1 \prec v_2$ in γ or $v_1 \prec v_2$ in γ' or $v_1 \in V'$ and $v \prec v_2$ in γ or $v_2 \in V'$ and $v_1 \prec v$ in γ .

A leaf that has a non-terminal label is called a *substitution node*.

Tree Substitution Grammars (3)



Tree Substitution Grammars (4)

Definition 2 (Tree Substitution Grammar)

A *Tree Substitution Grammar (TSG)* is a tuple $G = \langle N, T, S, I \rangle$ where

- N, T are disjoint alphabets of non-terminal and terminal symbols,
- $S \in N$ is the start symbol,
- I is a finite set of syntactic trees with labels from N and T .

Every tree in I is called an *elementary tree*.

G is called *lexicalized* if every tree in I has at least one leaf with a label from T .

Tree Substitution Grammars (5)

For a syntactic tree $\gamma = \langle V, E, r \rangle$ with node labeling functions l , we call $\langle V', E', r' \rangle$ with labeling functions l' an *instance* of γ if there exists a bijective function $h : V \rightarrow V'$ such that

- for all $v_1, v_2 \in V$: $\langle v_1, v_2 \rangle \in E$ iff $\langle h(v_1), h(v_2) \rangle \in E'$;
- for all $v_1, v_2 \in V$: $v_1 \prec v_2$ in γ iff $h(v_1) \prec h(v_2)$ in γ' ;
- for all $v \in V$: $l(v) = l'(h(v))$;

In other words, the two trees are isomorphic.

Tree Substitution Grammars (6)

In a derivation step, we select a node with a non-terminal label A , we pick a fresh instance of an elementary tree with root label A from the grammar and we substitute the node for the new tree.

Definition 3 (TSG derivation)

Let $G = \langle N, T, S, I \rangle$ be a TSG.

1. Let $\gamma = \langle V, E, r \rangle$ and γ' be syntactic trees.

γ' can be derived from γ in a single step, $\gamma \Rightarrow \gamma'$ if there is a node $v \in V$ and there is an instance $\gamma_e = \langle V_e, E_e, r_e \rangle$ of a tree from I such that

- $V \cap V_e = \emptyset$ (i.e., the node sets are disjoint),
- $\gamma' = \gamma[v, \gamma_e]$ (i.e., γ' is the result of substituting v for γ_e).

2. \Rightarrow^* is as usual the reflexive transitive closure of \Rightarrow .

Tree Substitution Grammars (7)

Definition 4 (TSG language)

Let $G = \langle N, T, S, I \rangle$ be a TSG.

1. We call a tree γ that can be derived from an instance of an elementary tree $\gamma_e \in I$ a *derived tree* in G .

2. The *tree language* of G is the set of all derived trees

$\gamma = \langle V, E, r \rangle$ in G such that

- $l(r) = S$, and
- $l(v) \in T \cup \{\varepsilon\}$ for every leaf $v \in V$.

3. For every tree γ with v_1, \dots, v_n being the leaves in γ ordered from left to right, we define $yield(\gamma) = l(v_1) \dots l(v_n)$.

4. The *string language* of G is $\{w \mid \text{there is a } \gamma \in L_T(G) \text{ such that } w = yield(\gamma)\}$.

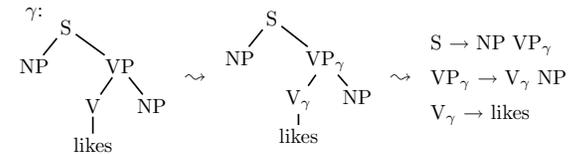
Equivalence of TSGs and CFGs (1)

In spite of the larger domains of locality, the following holds:

Proposition 1 (Equivalence of CFG and TSG) *CFG and TSG are weakly equivalent. Furthermore, except for some relabeling of the nodes, they are even strongly equivalent.*

1. Every CFG can be immediately written as a TSG with every production being understood as a tree with a single root and a daughter for every righthand side symbol
2. In order to construct an equivalent CFG for a given TSG, we have to encode the dependencies between nodes from the same tree within the non-terminal symbols.

Equivalence of TSGs and CFGs (2)



Applications

Even though TSGs are almost strongly equivalent to CFGs, they offer an extended domain of locality. This enables them to capture more generalizations than CFGs do.

- TSGs are used in the context of data-oriented parsing (DOP) [Bod et al., 2003].
- Lexicalized TSGs can be extracted from treebanks and used for probabilistic parsing [Post and Gildea, 2009].
- [Cohn et al., 2009] also induce [Probabilistic Tree Substitution Grammars](#) from treebanks and use them successfully for parsing.

References

- [Bod et al., 2003] Bod, R., Scha, R., and Sima'a, K., editors (2003). *Data-Oriented Parsing*. CSLI Publications, Stanford.
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- [Post and Gildea, 2009] Post, M. and Gildea, D. (2009). Bayesian learning of a tree substitution grammar. In *Proceedings of the ACL-IJCNLP 2009 Conference Short Papers*, pages 45–48, Singapore.