

Parsing

Homework 9 (LR), due 22 June 2020

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Question 1 (Canonical LR(1) construction and parse table)

1. Consider the CFG G with non-terminals $N = \{S\}$, terminals $T = \{a, b\}$, start symbol S and productions 1. $S \rightarrow Sa$, 2. $S \rightarrow aSb$, 3. $S \rightarrow \varepsilon$.

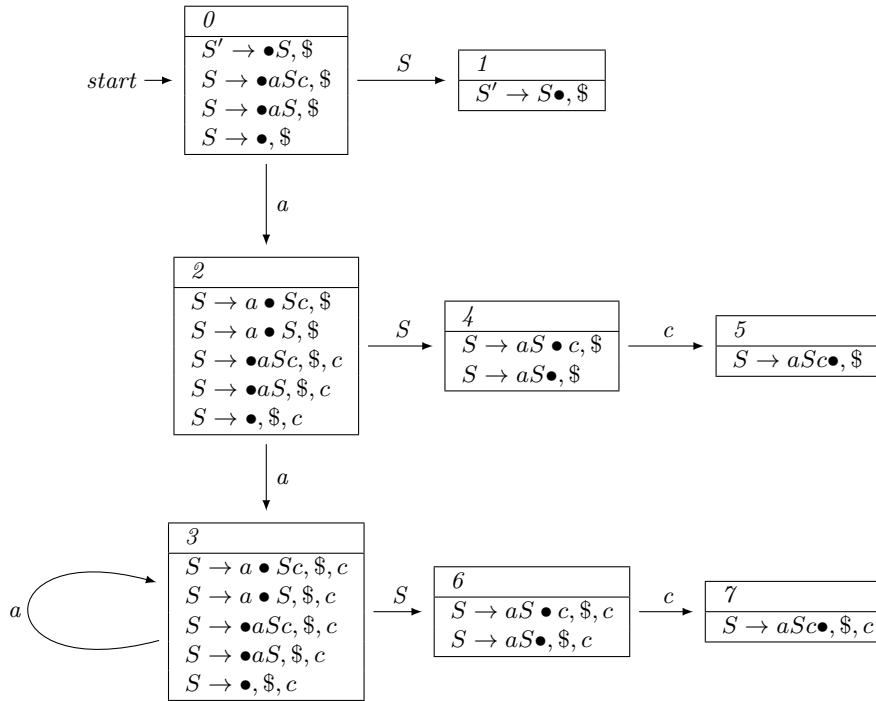
Consider the canonical LR(1)-construction for this grammar.

- (a) How does the state $q_0 = \text{closure}(\{S' \rightarrow \bullet S\})$ look like?
- (b) Give the state $q_1 = \text{goto} - \text{state}(q_0, a)$.
- (c) What would be the entry of the field for q_0 and a in the LR(1) action table?

2. Now consider the CFG $\langle N, T, P, S \rangle$ with

$N = \{S\}$, $T = \{a, c\}$, start symbol S , and productions 1. $S \rightarrow aSc$, 2. $S \rightarrow aS$, 3. $S \rightarrow \varepsilon$.

The LR(1)-automaton is as follows:



- (a) Give the LALR(1) automaton (states collapse that contain the same dotted productions, and all lookaheads are collected).
- (b) Read off the LALR(1) parse table.

Question 2 (Canonical LR(1) parsing)

Consider the CFG $G_4 = \langle N, T, P, S \rangle$ with $N = \{S, A, B, C\}$, $T = \{a, b, c\}$ and productions 1. $S \rightarrow ABC$, 2. $A \rightarrow a$, 3. $A \rightarrow aC$, 4. $B \rightarrow b$, 5. $B \rightarrow bC$, 6. $C \rightarrow c$.

It's LR(1) parse table with the canonical LR algorithm is as follows:

| | <i>a</i> | <i>b</i> | <i>c</i> | <i>§</i> | <i>A</i> | <i>B</i> | <i>C</i> | <i>S</i> |
|----|-----------|-----------|---------------|------------|----------|----------|----------|----------|
| 0 | <i>s1</i> | | | | 2 | | | 3 |
| 1 | | <i>r2</i> | <i>s11</i> | | | | 10 | |
| 2 | | <i>s5</i> | | | 4 | | | |
| 3 | | | | <i>acc</i> | | | | |
| 4 | | | <i>s7</i> | | | | 6 | |
| 5 | | | <i>s8, r4</i> | | | | 9 | |
| 6 | | | | <i>r1</i> | | | | |
| 7 | | | | <i>r6</i> | | | | |
| 8 | | | <i>r6</i> | | | | | |
| 9 | | | <i>r5</i> | | | | | |
| 10 | | <i>r3</i> | | | | | | |
| 11 | | <i>r6</i> | | | | | | |

1. Is this grammar LR(1)?
2. Give the shift-reduce parsing trace (i.e., the sequence of pairs of stack and remaining input) that we obtain for the input $w = abcc$.
If the parser is not LR(1) and the input cannot be parsed deterministically, list all possibilities.