Parsing

Hausaufgabe 1, Abgabe 12.04.2022 vor der Vorlesung, also vor 10.30 Uhr

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Question 1 (Grammars)

Consider the following three languages:

- $L_1 = \{a^n c d^m e^{n+3} \mid n, m > 0\}$
- $L_2 = \{a^k b c^n (cd)^m \mid k, n, m \ge 0\}$
- $L_3 = \{a^n (bcd)^{n-1} e^{n+1} \mid n \ge 2\}$

One of the languages is regular, one context-free and not regular and one not context-free. Which are the regular and the non-regular context-free languages? Justify your answer by giving the corresponding grammars.

Solution:

$$\begin{split} L_1 \text{ is context-free: } S &\to aSe \,|\, aTeee, T \to cD, D \to dD \,|\, d. \\ L_2 \text{ is regular: } S \to aS \,|\, bT, T \to cT \,|\, U, U \to cdU \,|\, \varepsilon. \end{split}$$

Question 2 (CFG) What are the CFLs generated by the following grammars?

1. G with non-terminals $N = \{S, T\}$, terminals $T = \{a, b, c\}$, start symbol S and productions

 $S \to aTba \,|\, aT, T \to S \,|\, c$

2. G with non-terminals $N = \{S\}$, terminals $T = \{a, b, c\}$, start symbol S and productions

 $S \rightarrow aSa \,|\, bSc \,|\, \varepsilon$

Solution:

- 1. $\{a^n c(ba)^m \mid n \ge m \ge 0, n > 0\}$
- 2. $\{w_1w_2 \mid w_1 \in \{a, b\}^*, w_2 = h(w_1^R) \text{ with } h(a) = a, h(b) = c\}$